COMMUTING AND

2-COMMUTING DERIVATIONS OF SEMIPRIME RINGS

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<u>Abstract</u>

The main purpose of this paper is to study and investigate some results concerning

generalized derivation D on semiprime ring R, we obtain a derivation d is commuting and 2-commuting on R.

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1 Introduction

This research has been motivated by the work of M.Ashraf[1]and M.A.Quadri, M.Shadab Khan and N.Rehman^[2]. The history of commuting and centralizing mappings goes back to (1955) when Divinsky [3] proved that a simple Artinian ring is commutative if it has a commuting nontrivial automorphism. Tow years later, Posner [4] has proved that the existence of a non-zero centralizing derivation on prime ring forces the ring to be commutative (Posner's second theorem).Luch [5]generalized the Divinsky result, we have just mentioned above, to arbitrary prime ring. Mayne [6] prove that in case

there exists a nontrivial centralizing automorphism on a prime ring, then the

ring is commutative (Mayne's theorem). Chung and Luh[7] have shown that every semicommuting automorphism of a prime ring is commuting provided that R has either characteristic different from 3 or non- zero center and thus they proved the commutativity of prime ring having nontrivial semicommuting automorphism except in the indicated cases Generalized derivation of operators on various algebraic structures have been an active area of research since the last fifty years due to their usefulness in various fields of mathematics.Some authors have studied centralizers in the general framework of semiprime rings (see[8,2,10,14,19,20,21,22,23and24]). Muhammad A.C.and Mohammed S.S.[16] proved.let R be a semiprime ring and $d: R \rightarrow R$ a mapping satisfy d(x)y=xd(y) for all $x, y \in R$. Then d is a centralizer. Molnar [15] has proved, let R be a 2-torsion free prime ring and let $d: R \rightarrow R$ be an additive mapping. If d(xyx)=d(x)yx holds for every $x,y \in R$,then is а left d centralizer.Muhammad A.C.and Α. B.Thaheem [17] proved , let d and g be a pair of derivations of semiprime ring R satisfying $d(x)x+xg(x) \in Z(R)$, then cd and cg are central for all $c \in Z(R).J.Vukman$ [24] proved, let R be a 2-torsion free semiprime ring and let

 $d: R \rightarrow R$ be an additive centralizing

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mapping on R, in this case, d is commuting on R.B.Zalar [24] has proved, let R be a 2torsion free semiprime ring and $d: R \rightarrow R$ an dditive mapping which satisfies $d(x^2) =$ d(x)x for all $x \in R$. Then d is a left centralizer.Hvala [11] initiated the algebraic study of generalized derivation and extended some results concerning derivation generalized to derivation.Majeed and Mehsin [12] proved, let R be a 2- torsion free semiprime ring, (D,d) and (G,g) be generalized derivations of R, if R admits to satisfy [D(x),G(x)]=[d(x),g(x)] for all $x \in \mathbb{R}$ and d acts as a left centralizer, then (D,d) and generalized (G,g)are orthogonal derivations of R.Recently, Mehsin Jabel [13] proved, let R be a semiprime ring and U be a non-zero ideal of R.If R admits a generalized derivation D associated with a non-zero derivation d such that D(xy) $yx \in Z(R)$ for all $x, y \in U$, then R contains a non-zero central ideal.Mehsin Jabel[8] proved, let R be a semiprime ring with left cancellation proprety,(D,d) and (G,g) be a non-zero generalized derivations of R.U a non-zero ideal of R, if R admists to satisfy [d(x),g(x)]=0 for all $x \in U$ and a non-zero d acts as a left centralizer (resp.a non-zero g acts as a left centralizer), then R contains a non-zero central ideal where two a dditive maps $d,g:R \rightarrow R$ are called orthogonal if d(x)Rg(y) = o=g(y)Rd(x) for \in R.And two generalized X.V all derivations (D,d) and (G,g) of R are called orthogonal if D(x)RG(y)=o=G(y)RD(x) for all $x, y \in R$, and we denote by (D,d) to a generalized derivation $D:R \rightarrow R$ determined by a derivation d of R .In this paper we study and investigate some results concerning generalized derivation D on semiprime ring R, we give some results about that.

2.Preliminaries

Throughout this paper, R will represent an associative ring with out identity and has a

cancellation property with the center Z(R). We recall that R is semiprime if xRx = (o) implies x=0 and it is prime if xRy=(0) implies x=0 or y=0.A prime ring is semiprime but the converse is not true in general. A ring R is 2-torsion free in case 2x = 0 implies that x = 0 for any $x \in \mathbb{R}$.An additive mapping d:R \rightarrow R is called a derivation if d(xy)=d(x)y+xd(y) holds for all $x, y \in R.A$ mapping d is called centralizing if $[d(x),x] \in Z(R)$ for all $x \in R$, in particular, if [d(x),x] = o for all $x \in R$, then it is called commuting, and is called central if $d(x) \in Z(R)$ for all $x \in R$. Every central mapping is obviously commuting but not conversely in general.In[10]Q.Deng and H.E.Bell extended the notion of commutativity to one of n-commutativity, where n is an arbitrary positive integer, by defining a mapping d to be n-commuting on U if $[x^n, d(x)]=0$ for all $x \in U$, where U be a non empty subset of R .Following Bresar [9] an additive mapping $D: R \rightarrow R$ is called a generalized derivation on R if there exists $d: R \rightarrow R$ such derivation that a D(xy)=D(x)y+xd(y)holds for all $x,y \in R$. However, generalized derivation covers the concept of derivation. Also with d=0,a generalized derivation covers the concept of left multiplier (left centralizer) that is,an additive mapping D satisfying D(xy) = D(x)y for all $x, y \in R$. As usual, we write [x,y] for xy–yx and make use of the commutator identities [xy,z]=x[y,z]+[x,z]yand [x,yz]=y[x,z]+[x,y]z, and the symbol xoy stands for the anti-commutator xy+yx. The following Lemmas are necessary for the paper

Lemma 2.1 [18,Corollary 9]

Any anticommutative semiprime ring R is commutative, where A ring R is said to be

anticommutative if xy=-yx (that is, xy + yx = 0) for all $x,y \in \mathbb{R}$.

3.The main results

Theorem 3.1

Let R be a semiprime ring.If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that D([x,y])=[x,y] for all $x,y \in$ R.Then d is commuting on R.

Proof: For $x,y \in R$,we have D([x,y])=[x,y] for all $x,y \in R$,which gives

 $\begin{array}{l} D(x)y+xd(y)-D(y)x-yd(x)-[x,y]=0\\ (1)\end{array}$

Replacing y by yz in (1), we obtain

Substituting (1) in (2) gives

D(y)[x,z]+yd(x)z+xd(y)z+xyd(z)-yd(z)x $yzd(x)-y[x,z]=0 \text{ for all } x,y \in \mathbb{R}.$ (3)

Replacing z by x in (3), we obtain

xd(y)x+xyd(x)-yxd(x)=0 for all $x,y \in R$. (4)

Replacing y by x in (4), we get

xd(x)x=0 for all $x \in R$. (5)

By using the cancellation property on x ,from left,we obtain

Again by using the cancellation property on x ,from right,we get

xd(x)=0 for all $x \in R$. (7)

Subtracting (6) and (7), we obtain

[d(x),x]=o for all $x \in R$. Thus ,d is commuting on R, by this we complete our proof.

A slight modification in the proof of the above theorem yields the following .

Theorem 3.2

Let R be a semiprime ring. If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that D([x,y])+[x,y]=0 for all $x,y \in$ R. Then d is commuting on R.

Theorem 3.3

Let R be a semiprime ring. If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that D(xoy)=(xoy) for all $x,y \in$ R. Then d is 2- commuting on R.

Proof:For any $x, y \in R$, we have

D(xoy)=(xoy) for all $x, y \in R$.

This can be written as

 $\begin{array}{ccc} D(x)y+xd(y)+D(y)x+yd(x)-(xoy) = 0 & \text{ for} \\ \text{all} & x,y & \in & R. \\ (8) & & \end{array}$

Replacing y by yx in above equation ,we obtain

According to (8) the relation above reduced to

(xoy)d(x)=0 for all $x,y \in \mathbb{R}$.

By using the cancellation property on d(x), we get

(xoy)=0 for all $x,y \in \mathbb{R}$. (10)

By Lemma 2.1, we get

 $[x,y]=0 \quad \text{for} \quad \text{all} \quad x,y \in \mathbb{R}.$ (11)

Replacing x by x^2 and y by d(x), we get

 $[d(x), x^2]=0$ for all $x \in R$. Thus, d is 2-commuting on R.

We complete our proof.

A slight modification in the proof of the Theorem(3.3) yields the following

Theorem 3.4

Let R be a semiprime ring. If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that D(xoy)+(xoy)=0 for all $x,y \in$ R. Then d is 2-commuting on R.

Proposition 3.5

Let R be a semiprime ring. If R admits a non-zero ideal generalized derivation D associated with a non-zero derivation d such that $D([x,y]) \pm (xoy)=0$ for all $x,y \in R$. Then 2-d is commuting on R.

Proof: For any $x, y \in \mathbb{R}$, we have

D([x,y])-(xoy)=0.Then

[D([x,y]),r]-[(xoy),r]=0 for all x,y,r $\in \mathbb{R}$.

Replacing y by x,we obtain

 $2[x^2,r]=0$ for all $x,r \in R.By$ using the cancellation property with replacing r by d(x)

,we obtain ,2-d is commuting on R.

Theorem 3.6

Let R be a semiprime ring. If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that d(x)oD(y)=0 for all $x,y \in$ R. Then d is commuting on R.

Proof: We have d(x)oD(y)=0 for all x, y \in R. (12)

Replacing y by yr,we obtain

(d(x)oy)d(r)-y[d(x),d(r)]+(d(x)oD(y))r-D(y)[d(x),r]=0 for all x,y \in U,r \in R. (13)

According to (12), then (13) reduced to

(d(x)oy)d(r)-y[d(x),d(r)]-D(y)[d(x),r]=0for all x, $y \in U, r \in \mathbb{R}$.

Replacing r by d(x), we get

 $\begin{array}{cccc} (d(x)oy)d^{2}(x)-y[d(x),d^{2}(x)]=0 & \text{ for all} \\ x,y & \in & R. \\ (14) & & \end{array}$

Replacing y by zy in (14), with using (14), we obtain

 $[d(x),z]yd^{2}(x)=0$ for all $x,y,z \in \mathbb{R}$. (15)

By using the cancellation property on (15) , from right, we obtain

[d(x),z]y=0 for all $x,y,z \in \mathbb{R}$. (16)

Since R is semiprime from above relation ,we get

 $\begin{bmatrix} d(x),z \end{bmatrix} = 0 \quad \text{for} \quad \text{all} \quad x,y \quad \in \quad \mathbb{R}.$ (17)

Replacing z by x,we obtain, d is commuting on R.

Theorem 3.7

Let R be a semiprime ring.If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that [d(x),D(y)]=0 for all $x,y \in R$. Then d is 2- commuting on R.

Proof: We have [d(x),D(y)]=0 for all x, y \in R. (18)

Replacing y by yz in(18) and using the result with (18), we obtain

D(y)[d(x),z]+y[d(x),d(z)]+[d(x),y]d(z)=0for all x,y \in R. (19)

Replacing z by zd(x) in (19) and using the result with (19), we get

 $yz[d(x),d^{2}(x)]+y[d(x),z]d^{2}(x)+[d(x),y]zd^{2}(x)=0$ for all $x,y \in \mathbb{R}$. (20)

Again replacing y by ry in (20) and using the result with (20), we obtain

 $[d(x),z]yd^{2}(x)=0$ for all $x,y,z \in \mathbb{R}$.

By using similar arguments as in the proof of Theorem 3.6, we obtain the required result.

Theorem 3.8

Let R be a semiprime ring. If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that d(x)oD(y)=xoy for all x,y \in R. Then d is 2-commuting on R.

Proof: For any $x, y \in R$, we have

d(x)oD(y)=xoy for all $x,y \in R$. Replacing y by yr, we get

(d(x)oy)d(r)-y[d(x),d(r)]+(d(x)oD(y))r-D(y)[d(x),r]= (xoy)r-y[x,r] for all x,y ,r \in R.Using our relation ,we obtain

 $\begin{array}{ll} (d(x)oy)d(r)-y[d(x),d(r)]-D(y)[d(x),r]\\ +y[x,r] &= 0 \quad \text{for all } x,y \quad ,r \in \mathbb{R}.\\ (21) \end{array}$

In (21) replacing r by d(x), we obtain

 $(d(x)oy)d^{2}(x)-y[d(x),d^{2}(x)]+y[x,d(x)]=0$ for all x,y \in R. (22)

Replacing y by zy in (22),we obtain

 $(z(d(x)oy)+[d(x),z]y)d^{2}(x)$ $zy[d(x),d^{2}(x)]+zy[x,d(x)]=0$ for all x,y \in R. (23)

According to(22), above relation reduced to

 $[d(x),z]yd^{2}(x)=0$ for all $x,y,z \in \mathbb{R}$. (24)

By using similar arguments as in the proof of Theorem 3.6, we obtain the required result.

A slight modification in the proof of the Theorem(3.8), yields the following

Theorem 3.9

Let R be a semiprime ring. If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that d(x)oD(y)+xoy=0 for all $x,y \in$ R. Then d is 2- commuting on R.

Theorem 3.10

Let R be a semiprime ring.If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that $d(x)D(y)-xy \in Z(R)$ for all x,y $\in R$. Then d is commuting on R.

Proof: For any $x, y \in R$, we have

d(x)D(y)-xy $\in Z(R)$,replacing y by yr,we obtain

 $\begin{array}{ll} (d(x)D(y)-xy)r+d(x)yd(r) \in Z(R) \ \text{for all} \\ x,y,,r \in & R. \\ (25) \end{array}$

This implies that

 $[d(x)yd(r),r]=0 \quad \text{for all} \quad x,y \quad ,r \in \mathbb{R}.$ (26)

Hence it follows that

 $\begin{aligned} &d(x)[yd(r),r]+[d(x),r]yd(r) = 0 & \text{ for all } x,y \\ &,r \in & R. \\ &(27) & \end{aligned}$

In (27) replacing y by d(x)y, we obtain

 $[d(x),r]d(x)yd(r)=0 \quad \text{for all } x,y,r \in \mathbb{R}.$ (28)

By using the cancellation property on d(x)yd(r), we obtain

 $[d(x),r]=0 for all x,r \in R.$ (29)

Replacing r by x in above relation, we obtain

 $[d(x),x]=0 for all x \in R.$ (30)

Then according to (30), we obtain

d is commuting on R.

By same method in above theorem ,we can prove the following

Theorem 3.11

Let R be a semiprime ring.If R admits a non-zero generalized derivation D

associated with a non-zero derivation d such that $d(x)D(y)+xy \in Z(R)$ for all x,y $\in R$. Then d is commuting on R.

Theorem 3.12

Let R be a semiprime ring. If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that [d(x),D(y)]=[x,y] for all $x,y \in$ R.Then d is 2- commuting on R.

Proof: For any $x, y \in R$, we have

 $[d(x),D(y)]=[x,y] \quad \text{for all } x,y \in \mathbb{R}.$ (31)

Replacing y by yz in (31), with using the result with (31), we obtain

Again replacing z by zd(x) in (32) with using the result with (32), we obtain

 $y[d(x),z]d^{2}(x)+yz[d(x),d^{2}(x)]+[d(x),y]zd^{2}(x)=yz[x,d(x)]$ for all $x,y \in \mathbb{R}$. (33)

Replacing y by ry in(33), we obtain

 $ryz[d(x),d^{2}(x)]+ry[d(x),z]d^{2}(x)+r[d(x),y]z$ $d^{2}(x)+[d(x),r]yzd^{2}(x)=ryz[x,d(x)]$

for all $x,y,r \in \mathbb{R}$. (34)

According to (33),the relation(34) reduced to

 $[d(x),r]yzd^{2}(x)=0$ for all $x,y,r \in \mathbb{R}$. (35)

Thus by same method in Theorem 3.6,we complete our proof.

Proceeding on the same lines with necessary variations, we can prove the following.

Theorem 3.13

Let R be a semiprime ring.If R admits a non-zero generalized derivation D associated with a non-zero derivation d such that [d(x),D(y)]+[x,y] = 0 for all x,y \in R.Then d is 2- commuting on R.

Remark 2.14

In general we can not obtain that d is non commuting where non satisfy the conditions which appear in our theorems ,the following example explain that .

Example 2.15

Let $R = \left\{ \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} / a^2 = b + a, a, b \in Z, the set of integers \right\}$ be a ring with cancellation property, and the additive map D define as the following

$$D \begin{pmatrix} \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & b \end{pmatrix} and d(x) = [a, x], where$$

$$a = \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} then, let$$

$$x = \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} and y = \begin{pmatrix} y & 0 \\ 0 & b \end{pmatrix} .then$$

$$D(xy) = D(x)y + xd(y)$$

$$D \begin{pmatrix} \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} \begin{pmatrix} y & 0 \\ 0 & b \end{pmatrix} = D \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} \begin{pmatrix} y & 0 \\ 0 & b \end{pmatrix} + \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} d \begin{pmatrix} y & 0 \\ 0 & b \end{pmatrix}$$

$$D \begin{pmatrix} ay & 0 \\ 0 & bh \end{pmatrix} = \begin{pmatrix} a & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} y & 0 \\ 0 & h \end{pmatrix} + \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} d \begin{pmatrix} y & 0 \\ 0 & h \end{pmatrix}$$

$$D \begin{pmatrix} ay & 0 \\ 0 & bh \end{pmatrix} = \begin{pmatrix} a & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} y & 0 \\ 0 & h \end{pmatrix} + \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} d \begin{pmatrix} y & 0 \\ 0 & h \end{pmatrix}$$

$$D \begin{pmatrix} ay & 0 \\ 0 & bh \end{pmatrix} = \begin{pmatrix} a & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} y & 0 \\ 0 & h \end{pmatrix} + \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} d \begin{pmatrix} y & 0 \\ 0 & h \end{pmatrix}$$

$$D \begin{pmatrix} ay & 0 \\ 0 & 0 \end{pmatrix} = \begin{pmatrix} ay & 0 \\ b(h - g) & 0 \end{pmatrix} = \begin{pmatrix} ay & 0 \\ 0 & 0 \end{pmatrix} .$$

$$D \begin{pmatrix} ay & 0 \\ b(h - g) & 0 \end{pmatrix} = b \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix},$$

then by using the cancellation property on \boldsymbol{b} , we get

$$\begin{pmatrix} 0 & 0 \\ h - g & o \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$
, which implies h=g

with substituting this result in equation (*), we obtain D is generalized derivation. Then we have

$$d(x)x = xd(x), where \ x = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

$$a < \infty > - \langle {}_{\mathcal{L}} \stackrel{\circ}{=} {}_{\alpha} \stackrel{\circ}{=} {}_{\alpha} \stackrel{\circ}{=} {}_{\alpha} \stackrel{\circ}{=} \stackrel{\circ}{=} {}_{\alpha} \stackrel{\circ}{=} \stackrel{\circ}{=} {}_{\alpha} \stackrel{\circ}{=} \stackrel{\circ}$$

In our theorems we cannot exclude the condition cancellation property , the following example explain that .

Example 2.17

Let
$$R = \left\{ \begin{pmatrix} x & y \\ 0 & z \end{pmatrix} / x, y, z \in Z, the set of integers \right\}.$$

be a ring with cancellation property ,and let m be fixed element of Z and the additive map D define as the following

$$\begin{split} D\left(\begin{pmatrix} x & y \\ 0 & z \end{pmatrix}\right) &= \begin{pmatrix} 0 & mx + mz \\ 0 & 0 \end{pmatrix}, \text{ and the derivation d defin as} \\ d\left(\begin{pmatrix} x & y \\ 0 & z \end{pmatrix}\right) \\ &= \begin{pmatrix} 0 & mx - mz \\ 0 & 0 \end{pmatrix}. \text{ then it is easy that D is generalized derivation on R. then} \end{split}$$

Then it is easy that D is generalized derivation

$$d(x)x = xd(x), where \ x = \begin{pmatrix} a & b \\ 0 & c \end{pmatrix} then$$

$$\begin{pmatrix} 0 & ma - mc \\ 0 & 0 \end{pmatrix} \begin{pmatrix} a & b \\ 0 & c \end{pmatrix} = \begin{pmatrix} a & b \\ 0 & c \end{pmatrix} \begin{pmatrix} 0 & ma - mc \\ 0 & 0 \end{pmatrix}$$

$$\begin{pmatrix} 0 & cma - mc^{2} \\ 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & ama & amc \\ 0 & 0 \end{pmatrix} (*)$$

$$\begin{pmatrix} 0 & m(ca - c^{2} - a^{2} + ac) \\ 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}, then$$

$$m \begin{pmatrix} 0 & 2ac - c^{2} - a^{2} \\ 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

$$m \begin{pmatrix} 0 & 2ac - c^{2} - a^{2} \\ 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

by using the cancellation property on $\begin{pmatrix} 0 & 2ac & c^2 & a^2 \\ 0 & 0 & 0 \end{pmatrix}$ we obtain

m = 0, therefore, by substituting this result in (*) give d is commuting.

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الملخص:الغرض الرئيسي من هذا البحث هو در اسة وتحري بعض النتائج بخصوص الاشتقاقات العامة D على الحلقات شبه الاولية R سوف نحصل على الاشتقاق D يكون ابدالي وابدالي -2 على R